

| Problem   | Section Name |
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| <p>1. The radius of a sphere is measured to be 5 cm with an error of <math>\pm 0.1</math> cm. Use differentials to approximate the error in volume.<br/>(A) <math>\pm \pi \text{ cm}^3</math> (B) <math>\pm 100\pi \text{ cm}^3</math> (C) <math>\pm 10\pi \text{ cm}^3</math> (D) <math>\pm 4\pi \text{ cm}^3</math> (E) <math>\pm 40\pi \text{ cm}^3</math></p>                             |              |
| <p>2. If <math>f(x) = \begin{cases} 2ax^2 + bx + 6, &amp; x \leq -1 \\ 3ax^3 - 2bx^2 + 4x, &amp; x &gt; -1 \end{cases}</math> and is differentiable for all real values, then <math>b = ?</math><br/>(A) <math>-13</math> (B) <math>0</math> (C) <math>45</math> (D) <math>55</math> (E) <math>110</math></p>   |              |
| <p>3. An equation of the line normal to the graph of <math>y = \sqrt{3x^2 + 2x}</math> at <math>(2, 4)</math> is<br/>(A) <math>-4x + y = 20</math> (B) <math>4x + 7y = 20</math> (C) <math>-7x + 4y = 2</math> (D) <math>7x + 4y = 30</math> (E) <math>4x + 7y = 36</math></p>  |              |
| <p>4. If <math>\cos^2 x + \sin^2 y = y</math>, then <math>\frac{dy}{dx} =</math><br/>(A) <math>\frac{2 \cos x \sin x}{2 \cos y \sin y + 1}</math> (B) <math>\frac{\cos x \sin x}{\cos y \sin y}</math> (C) <math>\frac{2 \cos x \sin x}{2 \cos y \sin y - 1}</math> (D) <math>\frac{\sin y \cos y}{1 - \cos x \sin x}</math> (E) <math>\frac{2 \cos y \sin y}{2 \cos x \sin x - 1}</math></p> |              |

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| <p>5. Find the volume of the region formed by the curve <math>y = x^2</math>, the <math>x</math> - axis and the line <math>x = 3</math> when revolved about the <math>y</math> - axis.</p> <p>(A) <math>\frac{3}{2}\pi</math> (B) <math>\frac{9}{2}\pi</math> (C) <math>\frac{27}{2}\pi</math> (D) <math>\frac{81}{2}\pi</math> (E) <math>\frac{243}{2}\pi</math></p>                                  |  |
| <p>*6. An open top cylinder has a volume of <math>125\pi \text{ in}^3</math>. Find the radius required to minimize the amount of material to make the cylinder.</p> <p>(A) 2 (B) 3 (C) 4 (D) 5 (E) 6</p>   |  |
| <p>*7. A 50 ft ladder is leaning against a building and being pulled to the ground, so the top is sliding down the building. If the rate the bottom ladder is being pulled across the ground is 12 ft/sec, what is the rate the top of the ladder is sliding down the building when the top is 30 ft from the ground?</p> <p>(A) 12 ft/sec (B) 9 ft/sec (C) 20 ft/sec (D) 9.6 ft/sec (E) 16 ft/sec</p> |  |
| <p>*8. If <math>f(x) = \left(1 + \frac{x}{20}\right)^5</math> find <math>f''(40)</math></p> <p>(A) 0.068 (B) 1.350 (C) 5.400 (D) 6.750 (E) 540.000</p>   |  |
| <p>*9. A particle height at time <math>t \geq 0</math> is given by <math>h(t) = 100t - 16t^2</math>. What is its maximum height?</p> <p>(A) 312.500 (B) 156.250 (C) 78.125 (D) 6.250 (E) 3.125</p>   |  |